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# The trade-off between taxi time & fuel consumption in airport ground movement

**Stefan Ravizza**

Jun Chen, Jason Atkin, Edmund Burke, Paul Stewart  
CASPT - S3.a: Fleet Logistics and Costs





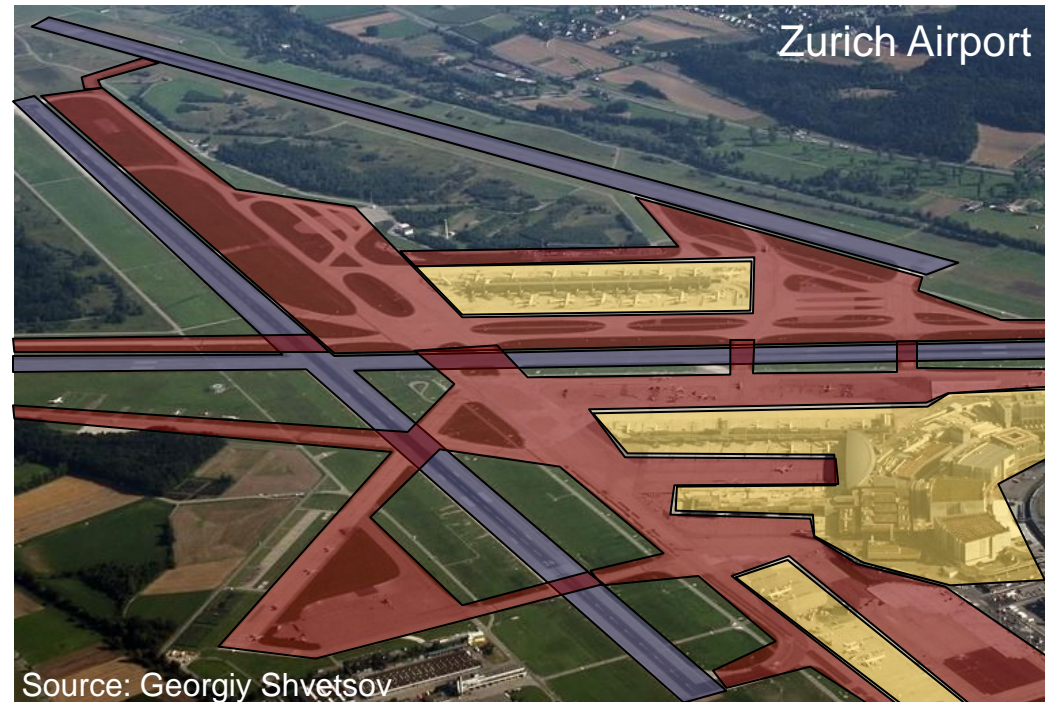
# Outline

- Airside airport operations
- Ground movement problem
  - » Sequential routing algorithm
- Is there potential to reduce fuel consumption?
  - » Concept of the new approach
- Results
  - » Analysis based on Zurich Airport data



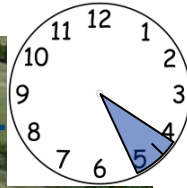
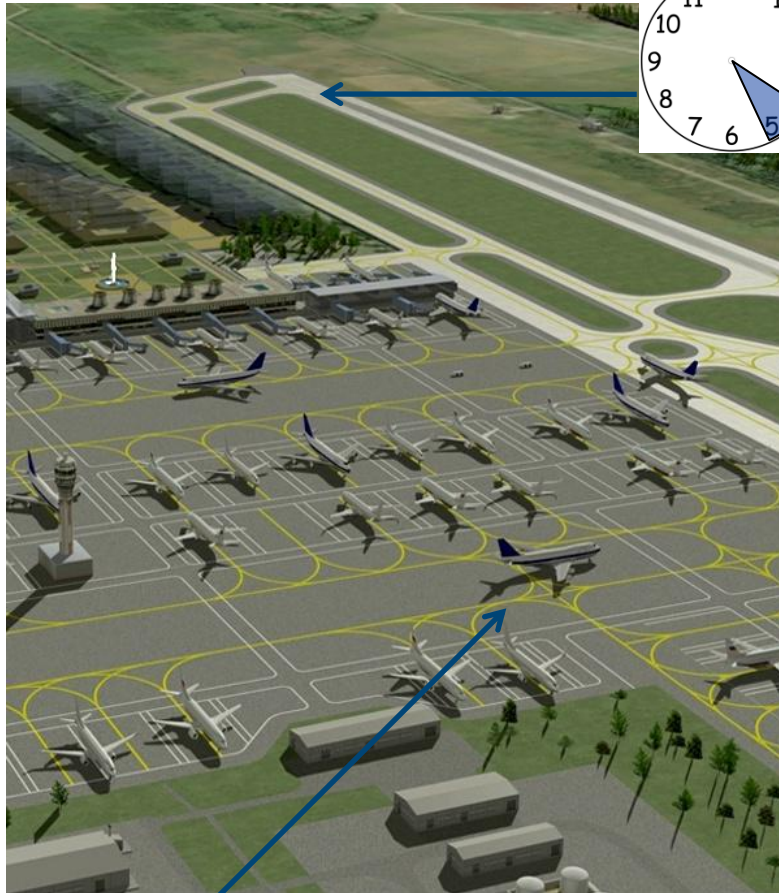
# Linked Airport Operations

- With increasing complexity and load at airports, more **advanced decision support systems** are needed
- Airside airport operations are **highly connected**
  - » Runway sequencing
    - Departures
    - Arrivals
  - » Gate assignment
  - » Ground movement

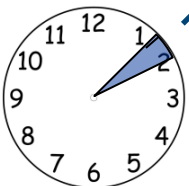




# Ground Movement Problem



- **Routing** and scheduling problem
- **Restrictions:**
  - » Set of possible routes
  - » Time windows for source and target
  - » Separations between aircraft
  - » Different movement speeds
- **Dynamic** nature



J. **Atkin**, E. **Burke**, and S. **Ravizza**, "The Airport Ground Movement Problem: Past and Current Research and Future Directions," *ICRAT*, Hungary, 2010.



# Routing Algorithm

- Sequential routing and scheduling approach
  - Minimises taxi time
  
- Quickest **P**ath **P**roblem with **T**ime-**W**indows (**QPPTW**)
  - Dijkstra on the underlying graph with labelling for the time-windows, respecting the edge reservations for all of the aircraft previously routed
  
- Absorbing waiting times for departures at stands  
→ **stand holding**

J. **Atkin**, E. **Burke**, and S. **Ravizza**, “A more realistic approach for airport ground movement optimisation with stand holding,” *MISTA*, USA, 2011.



# Can we do better?

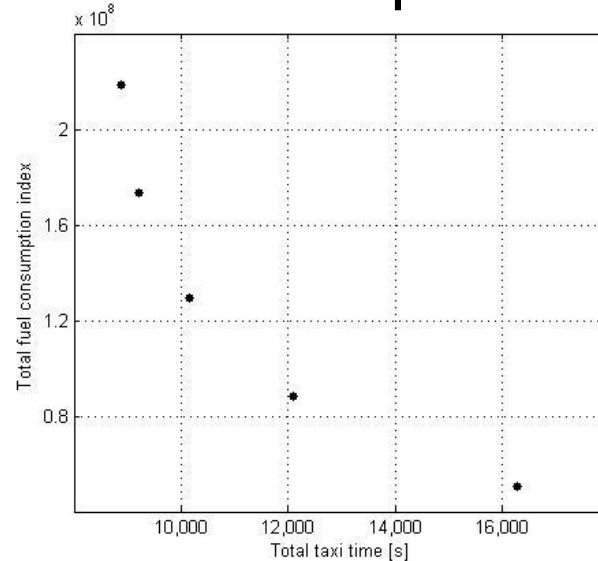
Source: Flughafen Zürich AG





# Concept at a Glance

- **Output:** global discretised pareto-front



- Framework:
  1. Loop for each **objective function** discretisation
  2. Loop for each **aircraft**

# k-QPPTW

- Finding the best  $k$  routes w.r.t. minimal taxi time using the k-QPPTW algorithm





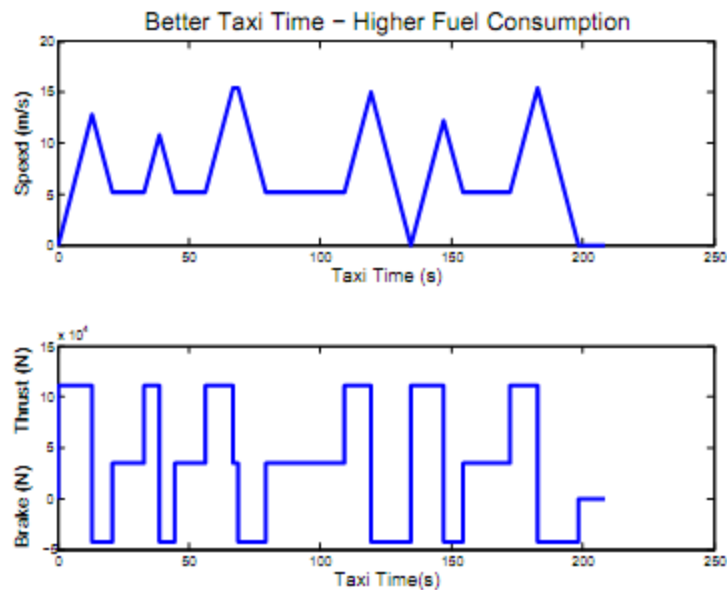
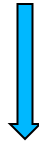
# Population Adaptive Immune Algorithm

- Loop for each of the  **$k$  routes** of an aircraft
  - » Approximate the pareto-front of both objectives, using the population adaptive immune algorithm
- Considering “**time-efficiency**” & “**fuel-efficiency**”
- **Aircraft models** link acceleration, deceleration, and speed to taxi-time and fuel burn
- Taking reservations into account

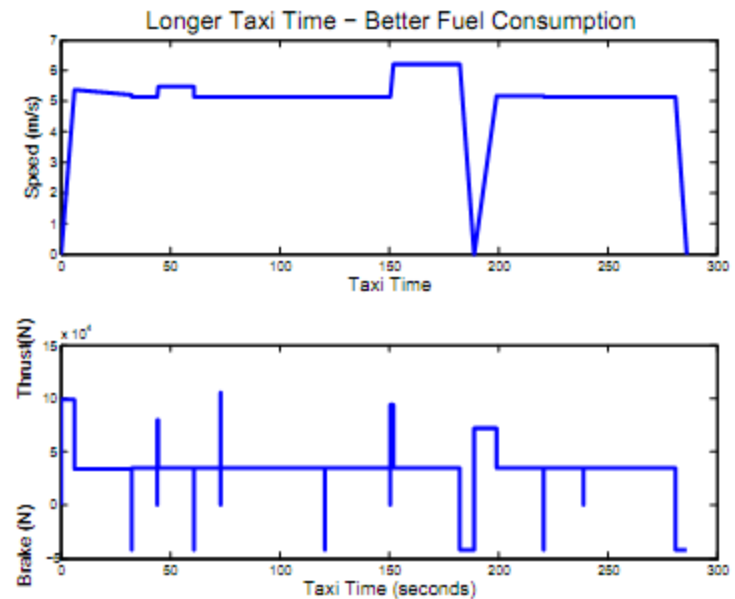
J. **Chen**, P. **Stewart**, “Planning aircraft taxiing trajectories via a multi-objective immune optimisation”, *ICNC*, China, 2011.

# Trajectories

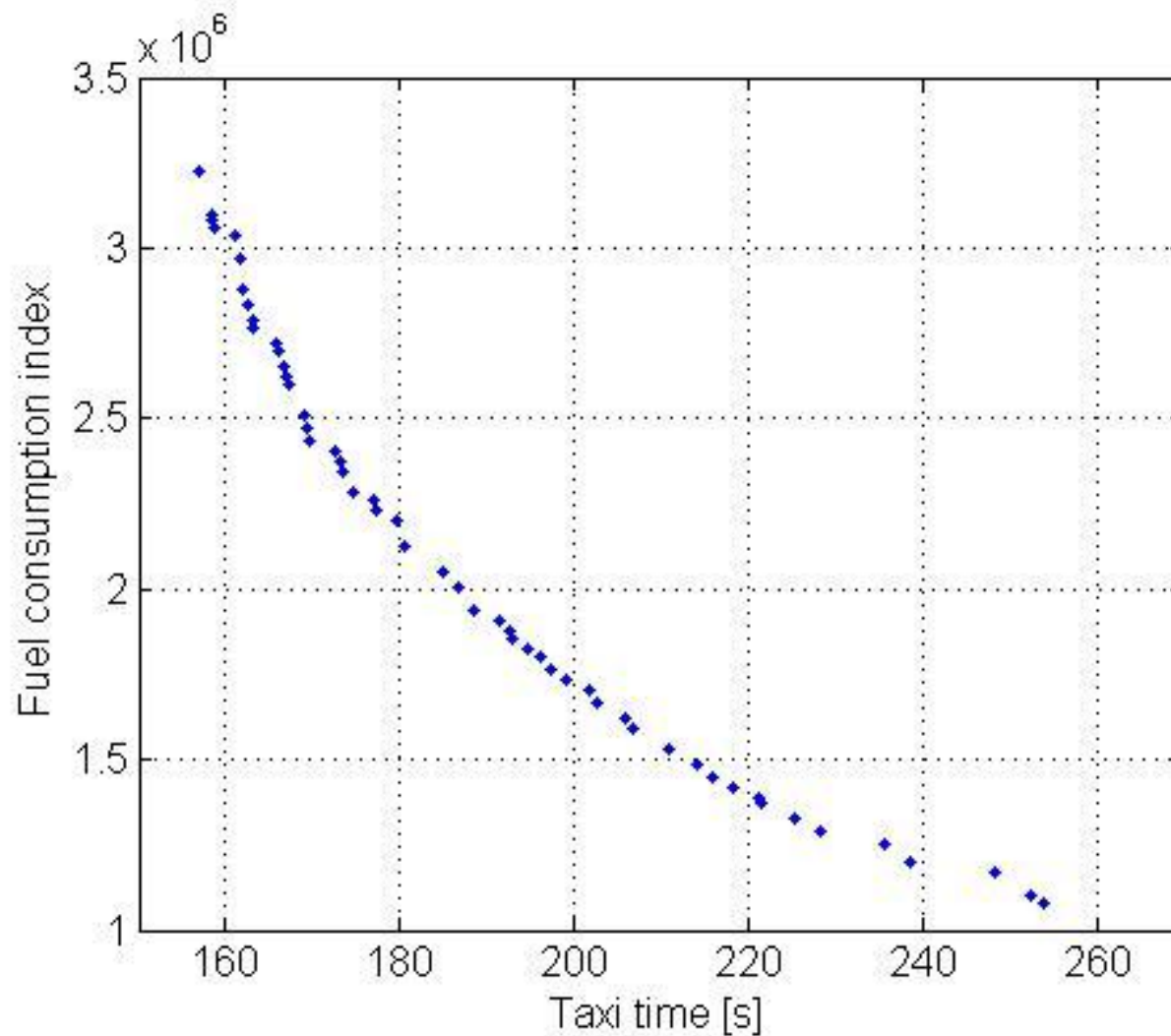
## Time-efficient



## Fuel-efficient

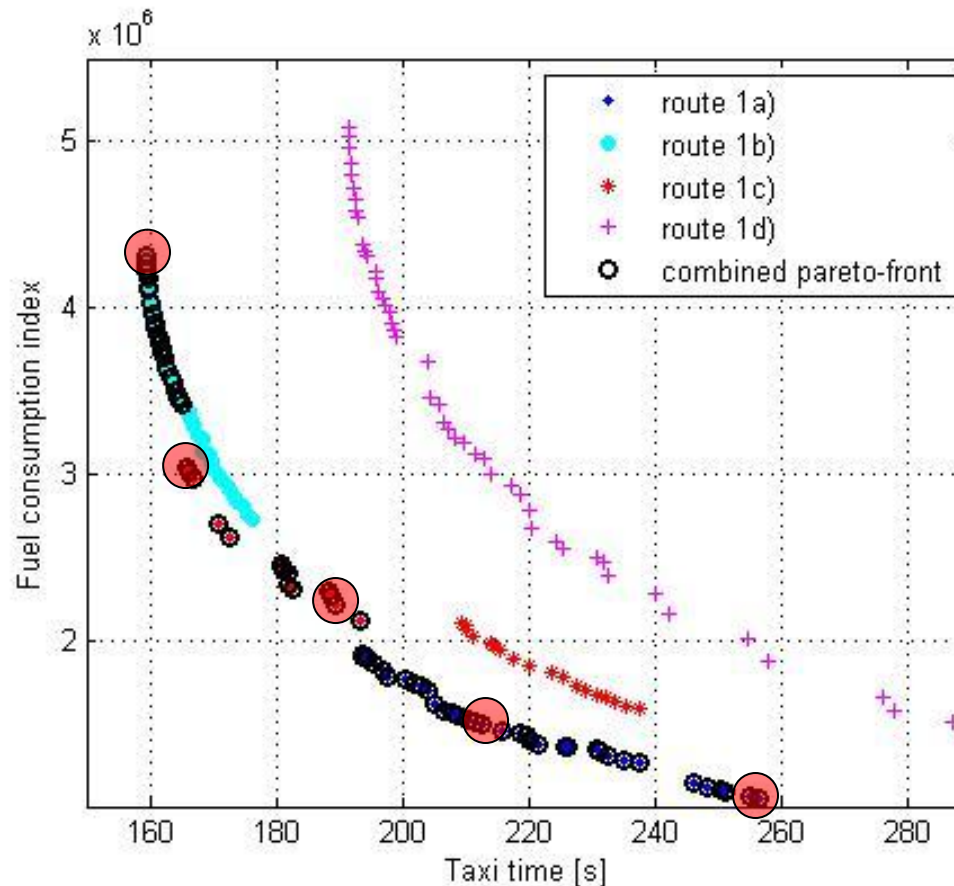


# Pareto-front of a Route



# Combined Pareto-front

- Plot of 4 different routes
- Combined pareto-front with discretisation





# Pseudocode

```
1 Sort all flights by pushback/landing time
2 foreach objective function discretisation  $i \leftarrow 1$  to  $l$  do
3   foreach aircraft  $a$  do
4     Find the best  $k$  routes w.r.t. minimal taxi times using the  $k$ -QPPTW
       algorithm
5     foreach route  $k$  of aircraft  $a$  do
6       Approximate the pareto-front of both objectives, using the population
       adaptive immune algorithm (PATT-PAIA)
7     Generate the combined pareto-front for the source-destination pair of
       aircraft  $a$ 
8     Discretise this pareto-front into  $l$  roughly equally spaced points
9     Select the  $i$ th point and reserve the relevant route for aircraft  $a$ 
10  Save the accumulated values for all aircraft for both objective functions for the
    global pareto-front
11 Output: Global discretised pareto-front
```



# Results

- One week's operation at Zurich Airport
- 2. objective function:  $F_{Total} = F_{Resistance} + F_{Acceleration}$

	Mon	Tue	Wed	Thu	Fri	Sat	Sun
<b>Ø Taxi time</b>							
Time-efficient [s]	156	157	128	174	152	165	154
Fuel-efficient [s]	285	293	214	320	292	316	295
Growth	83%	87%	67%	84%	92%	91%	91%
<b>Ø Fuel cons. index</b>							
Time-efficient [ $\times 10^3$ ]	3832	3291	3492	4002	3173	3754	3718
Fuel-efficient [ $\times 10^3$ ]	884	762	742	922	700	849	823
Growth	334%	332%	371%	334%	353%	342%	352%
Number of aircraft	57	58	46	58	56	63	52



# Different Objective Function

- 2 different phases:
  - » Acceleration (10% of maximal fuel flow)
  - » Taxiing with constant speed, deceleration, holding (5.5%)

	Different objective function
Ø <b>Taxi time</b> Time-efficient [s] Fuel-efficient [s] Growth	155.5 156.7 0.8%
Ø <b>Fuel flow</b> Time-efficient [kg] Fuel-efficient [kg] Growth	23.8 23.5 1.2%

M.E.J. Stettler, S. Eastham, S.R.H. Barrett, "Air quality and public health impacts of UK airports. Part I: Emissions", *Atmospheric Environment*, 45(31), 2011.



# Summary

- **Novel concept** using combined:
  - » k-QPPTW
    - Finds best possible routes for an aircraft
  - » Population adaptive immune algorithm
    - Finds approximation of the pareto-front for different speed profiles for each of these routes
- **Trade-off**
  - » Depends very much upon the actual modelling of the fuel-based obj. function (physics-based vs. fuel flow)
  - » These appears not to be well understood



# My References

## Published / accepted:

- “The airport ground movement problem: Past and current research and future directions”, In Proceedings of the 4th International Conference on Research in Air Transportation (**ICRAT 2010**), Budapest, Hungary, pages 131–138, 2010.
- “A statistical approach for taxi time estimation at London Heathrow Airport”, In Proceedings of the 10th Workshop on Models and Algorithms for Planning and Scheduling Problems (**MAPSP 2011**), Nymburk, Czech Republic, pages 61–63, 2011.
- “A more realistic approach for airport ground movement optimisation with stand holding”, In Proceedings of the 5th Multidisciplinary International Scheduling Conference (**MISTA 2011**), Phoenix, Arizona, USA, pages 146-160, 2011.
- “On the utilization of fuzzy rule-based systems for taxi time estimations at airports”, In Proceedings of the 11th Workshop on Algorithmic Approaches for Transportation Modelling, Optimization, and Systems (**ATMOS 2011**), Saarbrücken, Germany, pages 134-145, 2011.
- “Exploration of the ordering for a sequential airport ground movement algorithm”, Technical Report, 1543, University of Nottingham, 2011.
- “Trade-off between taxi time and fuel consumption in airport ground movement”, Accepted for the Conference on Advanced Systems for Public Transport (**CASPT 2012**)

## Submitted:

- “A statistical approach for improving taxi time estimations at airports”, Submitted to a journal.
- “A more realistic approach for airport ground movement optimisation with stand holding”, Submitted to a journal.



# Contact Details

**Stefan Ravizza**

PhD Student

smr@cs.nott.ac.uk

<http://www.asap.cs.nott.ac.uk/atr/>



The University of  
**Nottingham**

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